



 If white light is shone through a prism, it is *diffracted* to produce a *continuous spectrum* of colours; red, orange, yellow, green, blue, indigo and violet.





• If atoms and molecules are heated to sufficiently high temperatures, they emit light of certain wavelengths.



• The diagram below shows a discharge tube containing a gaseous element. Note the spectrum that is produced is a *discrete spectrum*, not a *continuous spectrum*.



• The observed spectrum consists of a number of coloured lines on a black background. The spectrum is called an *atomic emission spectrum* or *line spectrum*.





• The atomic emission spectra of gaseous *mercury*, *lithium*, *cadmium*, *strontium*, *calcium* and *sodium*:



 The visible spectrum of *hydrogen* consists of 4 bands of light of specific wavelengths. This spectrum is generated when gaseous hydrogen is excited by an electrical current and the light given off by the gas is split by a prism.

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 Viewed through a spectrometer, the emission spectrum of hydrogen is seen to be a number of separate sets of lines, or a series of lines. Each series of lines is named after the scientist who discovered them as shown in the diagram below:



 A more detailed view of the *Balmer* series of hydrogen is shown in the diagram below:



 Note how the intervals between the frequencies of the lines becomes smaller and smaller towards the higher frequency end of the spectrum until the lines converge together to form a continuous spectrum of light.

- Why do atoms absorb or emit light of certain frequencies?
 - Why do atomic spectra consist of discrete (separate) lines?
- Why do the spectral lines converge at higher frequencies to form a continuous spectrum?



Niels Bohr
(1885 – 1962)
Nobel Prize
for Physics
1922.

 In 1913, Niels Bohr put forward his structure of the atom to answer these questions. Bohr referred to Max Planck's recently discovered quantum theory,

according to which energy can be absorbed or emitted in certain amounts, like separate packets of energy, called *quanta*.



Max Planck
(1858 – 1947)
Nobel Prize
for Physics
1918.



• Niels Bohr and Albert Einstein.

• Niels Bohr suggested the following:

 An electron moving in an orbit can only have certain amounts of energy, not an infinite number of values, *i.e.* the electron's energy is *quantised*.

2) The energy that an electron needs to move in a particular orbit depends upon the radius of the orbit. An electron that is moving in an orbit *distant* from the nucleus has a *higher* energy compared to an electron that is moving in an orbit near to the nucleus of the atom.

3) If the energy of the electron is quantised, then the radius of the orbit must also be quantised. An atom therefore contains a restricted number of orbits, not an infinite number of orbits.

4) An electron moving in one of these orbits does not emit energy. In order to move to an orbit further away from the nucleus, the electron must *absorb* energy to do work against the attraction of the nucleus. If an atom absorbs a *photon* of light, then the absorbed energy can promote (*excite*) an electron from an inner orbit to an outer orbit. When an electron falls (*relax*) from a higher orbit to a lower orbit, then energy is *released* as a photon of light.

 For an electron to move from an orbit of energy E₁ to E₂, the light absorbed must have a frequency given by *Planck's equation*:

 $hv = E_2 - E_1$ where v = frequency and h = Planck's constant.



• The emission spectrum arises when electrons which have been excited (raised into orbits of higher energy) fall back to orbits of lower energy. As these electrons relax, they emit energy as light with a frequency given by Planck's equation.



 Bohr assigned *quantum numbers* to the orbits. He gave the orbit of lowest energy (closest to the nucleus) the quantum number 1. An electron in this orbit is said to be in its *ground state*. The next energy level has a quantum number of 2.





 The emission spectrum of hydrogen arises when the electron in its ground state absorbs energy and is excited into a higher energy orbit. When the electron relaxes into a lower energy orbit, it releases energy as light with a frequency given by Planck's equation:

hv = E2 - E1





 Arnold Sommerfeld (1868 – 1951) and Niels Bohr. Arnold Sommerfeld elaborated on Bohr's theory in1916. He proposed that each quantum number governed the energy of a circular orbit and also a set of *elliptical orbits* of similar energy.



• Sommerfeld also called *n* the *principle quantum number* and introduced a second quantum number to describe the shapes of the elliptical orbits.

The second quantum number, *I*, can have values from (*n* – 1) down to *O*. For example, if *n* = 4, then the values of *I* would be 3,2,1 and 0.



 Louis de Broglie (1892 – 1987)
Awarded the Nobel Prize for Physics in 1929.

 According to the wave theory of light, refraction and diffraction can be explained by the properties of waves. Other properties of light, such as the origin of line spectra and the photoelectric effect need a particle or photon theory for their explanation. The success of the duel theory of light led Louis de Broglie to speculate in 1924 on whether particles might have wave properties. He made the bold suggestion that electrons have wave properties as well as the properties of particles.



 Erwin Schrödinger (1887 – 1961)
Awarded the Nobel Prize for Physics in 1933.



 Paul Dirac (1902 – 1984)
Awarded the Nobel Prize for Physics in 1933.

 Erwin Schrödinger and Paul Dirac used de Broglie's theory to work out a wave theory for the atom. One version of Schrödinger's famous wave equation is given below:

$$\frac{\delta^2 \Psi}{\delta x^2} + \frac{\delta^2 \Psi}{\delta y^2} + \frac{\delta^2 \Psi}{\delta z^2} + \frac{8m\pi^2}{h^2} (E - V)\Psi = 0$$

• The solution to the wave equation gives the *probability density* of the electron. This is the probability that the electron is present in a small given region of space.



• The graph on the left shows a probability density diagram for a hydrogen atom in its ground state. The maximum probability of finding an electron is 0.053 nm from the nucleus.



• There is a possibility that the electron will be either closer to the nucleus or outside the radius of 0.053 nm. The probability of finding the electron decreases sharply as the distance from the nucleus increases beyond 3r.



 The volume of space in which there is a 95% probability of finding the electron is called the atomic orbital.

 Solutions of the wave equation can be obtained if the orbitals are described by *four quantum numbers*.

• The first is Bohr's principle quantum number, *n*.

• The second quantum number, *I*, corresponds to Sommerfeld's quantum number describing the shape of the elliptical orbits. The values of *I* are assigned letters:

$$l = 0 = s$$

 $l = 1 = p$
 $l = 2 = d$
 $l = 3 = f$

 If an electron has a principle quantum number n = 2 and a second quantum number l = 0, it is said to be a 2s electron. For various values of n, the different combinations of the two quantum numbers are:

> 1s 2s 2p 3s 3p 3d 4s 4d 4d 4f

 Schrödinger's wave equation leads to a third quantum number, m_l. This gives the maximum number of orbitals for the different values of *I*:

> One s-orbital Three p-orbitals Five d-orbitals Seven f-orbitals

• The fourth quantum number is called the spin quantum number, m_s . It has values of $+\frac{1}{2}$ and $-\frac{1}{2}$ and represents the spin of the electron on its own axis.







 Wolfgang Pauli (1900 – 1958)
Awarded the Nobel Prize for Physics in 1945.

 Pauli's exclusion principle states that no two electrons in an atom can have the same four quantum numbers. It therefore follows that if two electrons in an atom have the same values of *n*, *l*, and *m_l*, they must have different values of m_s , *i.e. their spins must be opposed.* The consequence of this is that an orbital can hold a maximum number of *two electrons* with opposite spins.
The shape of an *s-orbital* is *spherically symmetrical* about the nucleus. The orbital has no preferred direction. The probability of finding an electron at a distance *r* from the nucleus is the same in all directions.



 A *p-orbital* is concentrated in certain directions.
 p-orbitals exits in groups of *three* arranged at 90° to each other.



• *d-orbitals* are arranged in groups of *five*.







 The term shell is used for a group of orbitals with the same principle quantum number (n). A sub-shell is a group of orbitals with the same principle and second quantum numbers (n and l), e.g. the 3p subshell.

- When writing out the electron configurations of atom, it is convenient to remember the following:
- → Electrons should fill orbitals from the *lowest energy* to the *highest energy* (known as the *Aufbau principle*).
 - \rightarrow The Pauli Exclusion Principle no two electrons in the same atom can have the same four quantum numbers.
 - \rightarrow Orbitals fill-up in the order 1s, 2s, 2p, 3s, 3p, 4s, 3d, 4p.



 For convenience, orbitals are often drawn as *boxes*.

 Each orbital can hold a maximum number of two *electrons*. These are represented by drawing arrows in the boxes, one arrow pointing up and one arrow pointing down to represent the opposite spin.

energy



- s-orbitals (red) are represented by a single box.
- *p-orbitals* (blue) are represented by a group of three boxes.
- *d-orbitals* (green) are represented by a group of five boxes.



 This diagram shows the order in which the orbitals fill-up, from the lowest energy to the highest energy.

> *et cetera* 3*d* ↑ 4*s* ↑ 3*p* ↑ 3*s* ↑ 2*p* ↑ 2*s* ↑ 1*s*

 It is convenient to draw "electrons in boxes" diagrams to show the arrangement of electrons in orbitals. Arrows are used to represent the electrons. Arrows pointing in opposite directions represent electrons with opposite spin.

1 – Hydrogen





 It is convenient to draw "electrons in boxes" diagrams to show the arrangement of electrons in orbitals. Arrows are used to represent the electrons. Arrows pointing in opposite directions represent electrons with opposite spin.

2 – Helium



 It is convenient to draw "electrons in boxes" diagrams to show the arrangement of electrons in orbitals. Arrows are used to represent the electrons. Arrows pointing in opposite directions represent electrons with opposite spin.

3 – Lithium





 It is convenient to draw "electrons in boxes" diagrams to show the arrangement of electrons in orbitals. Arrows are used to represent the electrons. Arrows pointing in opposite directions represent electrons with opposite spin.

4 – Beryllium





 It is convenient to draw "electrons in boxes" diagrams to show the arrangement of electrons in orbitals. Arrows are used to represent the electrons. Arrows pointing in opposite directions represent electrons with opposite spin.

5 – Boron



• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

5 – Boron



• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

6 – Carbon





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

7 – Nitrogen





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

8 – Oxygen





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

9 – Fluorine





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

10 – Neon





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

11 – Sodium





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

12 – Magnesium





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

13 – Aluminium





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

14 – Silicon





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

15 – Phosphorus





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

16 – Sulfur





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

17 – Chlorine





• Note: Because electrons all carry a charge of -1, they naturally repel each other. Because of this, when electrons enter p-orbitals, they will initially occupy separate p-orbitals before they are forced to pair-up (*spin-pair*) with each other.

18 – Argon





• The electron configuration of carbon is given below:

Carbon



Questions:

From the electron configuration shown above, how many covalent bonds would you expect a carbon atom to make?
How is it possible for a carbon atom to make *four* covalent bonds?

• Carbon (*ground state*):

Carbon (*excited*):



Carbon (sp³ hybridised):

• Carbon (*ground state*):

Carbon (sp³ hybridised):

Carbon (*excited*):



• Carbon makes four covalent bonds.

• Key: \uparrow = electron of carbon \downarrow = electron of another chemical element.



• The *sp*³ hybridisation of carbon.



• The bonding in methane (CH₄).

 The four sp³
 hybridised orbitals of the carbon atom (blue) overlap with the s-orbitals of four hydrogen atoms (red) to form four σ-bonds.



Carbon (*excited*):



Carbon (sp² hybridised):



Carbon (sp² hybridised):





• Carbon makes four covalent bonds.

• Key: \uparrow = electron of carbon \downarrow = electron of another chemical element.



• The bonding in ethene (C_2H_4) #1.

 The three sp²
 hybridised orbitals of each carbon atom (blue) overlap with each other and also with the s-orbitals of four hydrogen atoms (red) to form a total of five σ-bonds.



• The bonding in ethene (C_2H_4) #2.

• The *p*-orbitals of each carbon atom which are not hybridised (green) are arranged parallel to each other. They overlap above and below the plane of the molecule forming a π -bond.
σ -Bonds and π -Bonds



• A comparison of σ -bonds and π -bonds:

• σ -bonds are formed when the region of orbital overlap lies directly between the nuclei of the two bonding atoms.

• π -bonds are formed when the region of orbital overlap does not lie directly between the nuclei of the two bonding atoms, but instead lies above and below the plane of the molecule.

The Existence of $C \equiv C$ Bonds

Question:

 Elaborate on this information to propose a model for the bonding in ethyne:



Your answer should take into account:

→ The existence of s-orbitals and p-orbitals.
→ The ability for carbon's 2s and 2p orbitals to hybridise.
→ The linear shape of the ethyne molecule.

• Carbon (*ground state*):

Carbon (*excited*):



• Carbon (sp hybridised):

• Carbon (*ground state*):

Carbon (sp hybridised):

Carbon (*excited*):



• Carbon makes four covalent bonds.

• Key: \uparrow = electron of carbon \downarrow = electron of another chemical element.



• The bonding in ethyne (C_2H_2) #1.

• The sp hybridised orbitals of each carbon atom (blue) overlap with each other and also with the s-orbitals of two hydrogen atoms (red) to form a total of three σ -bonds arranged in a linear formation.

(c) Hybridization and bonding scheme

 $\pi: C(2p) - C(2p)$

 σ : H(1s) — C(sp)



(c) Hybridization and bonding scheme

• The bonding in ethyne (C_2H_2) #2.

 Each carbon atom has two p-orbitals (green) which are not hybridised. They arranged at 90° to each other within the same carbon atom and parallel to each other between the individual carbon atoms. Overlap of the four p-orbitals results in the formation of two π -bonds between the two carbon atoms.

A Summary of sp³, sp² and sp Hybridisation



- The carbon atoms forming a C C bond are sp^3 hybridised.
- The carbon atoms forming a C = C bond are sp^2 hybridised.
- The carbon atoms forming a $C \equiv C$ bond are sp hybridised.

Question:

 With this information, propose a structure for benzene, formula C₆H₆, which takes into account:

→ The existence of *s*-orbitals and *p*-orbitals.
→ The ability for carbon's 2s and 2p orbitals to hybridise.
→ The shape of the benzene molecule as determined by *x*-ray crystallography.
→ The relative stability of benzene.



• The structure of benzene (C_6H_6) determined by x-ray crystallography. Note: the six carbon atoms are arranged in a planar six-membered ring and all of the carbon-to-carbon covalent bonds are the same length.

• Carbon (ground state):

Carbon (*excited*):



Carbon (sp² hybridised):

Carbon (ground state):

Carbon (sp² hybridised):

Carbon (*excited*):



• Carbon makes four covalent bonds.

• Key: \uparrow = electron of carbon \downarrow = electron of another chemical element.

Carbon atom in *benzene*:



• Carbon atom in *benzene*: $\uparrow \downarrow \uparrow \uparrow \uparrow \uparrow$ \uparrow

 σ -bond to carbon.









• The structure of benzene #1.

 All six of the carbon atoms in benzene are sp² hybridised. This results in *σ-bonding* between the sp² hybridised orbitals of carbon (blue) and the *s-orbitals* of hydrogen (red).



• The structure of benzene #2.

 The *p*-orbitals of carbon which are not hybridised (purple) are arranged parallel to each other and overlap both above and below the plane of the benzene ring forming a cloud of *delocalised of π*-bonding electrons.



 Delocalisation of the π-bonding electrons around the benzene ring lowers the energy of the structure by approximately 150 kJ mol⁻¹, a value often referred to as the delocalisation enthalpy.



• A cloud of *delocalised* π -bonding electrons exists above and below the plane of the benzene ring.



 Benzene is a regular, planar hexagon in which all of the bond angles are 120° and all of the carbon-tocarbon covalent bond lengths are 0.139 nm.





Quantum mechanics.

Quantum Theory of Atomic Structure

Presentation on Quantum Theory of Atomic Structure by Dr. Chris Slatter christopher_john_slatter@nygh.edu.sg

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